
Complexity of Algorithms

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8.1 Computational Complexity

In this chapter, we see how problems may be classified according to their level of difficulty.

Most problems that we consider in this book are of a general character, applying to all members of some family of graphs or digraphs. By an *instance* of a problem,